

Comment on "Percolation Thresholds in the Three-Dimensional Stick System"

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We discuss a classical mistake made in earlier publications on the stick percolation problem in 3D for generating the right isotropic configuration of sticks. We explain the observed systematic deviations from the excluded volume rule. New MC simulations considered by us confirm nicely the applicability of the excluded volume theory.

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The three-dimensional continuum percolation problem of permeable sticks with the form of capped cylinders was considered by Monte Carlo simulations in Ref. [1]. The authors report the dependence of the percolation threshold on aspect ratio and on macroscopic anisotropy, discussing the results from the viewpoint of the excluded volume theory [2].

Throughout the paper [1] the authors claim to obtain the isotropic distribution of the rods orientations by generating their θ and φ polar coordinates randomly with a uniform distribution on the $[-\pi/2, \pi/2]$ and $[0, 2\pi]$ intervals, respectively. Following their two-dimensional study [3] they define the measure of the macroscopic anisotropy of the system as:

$$P_{\parallel}/P_{\perp} = \frac{\sum_{i=1}^N |\cos(\theta_i)|}{\sum_{i=1}^N [1 - \cos^2(\theta_i)]^{1/2}} \quad (1)$$

However, proceeding in the way described above, the generated configurations will definitely not be the isotropic ones, although their anisotropy constant (1) will be. It is easy to realize that the z axes will be a privileged one, and percolation in this direction reached easier than in the y or x direction. In order to get the right isotropic distribution for the rods orientation, their endpoints must span uniformly the surface of a sphere. This can be achieved only by choosing the θ angle randomly with a weighted distribution and not a uniform one. From the surface element on the unit-sphere ($d\sigma = \sin(\theta) d\theta d\varphi$) it is immediate to realize that the weight-factor is governed by the $\sin(\theta)$ term.

The mistake made by the authors does not effect the $L \ll r$ (L the length of the cylinder and r its radius) limit, considered by the authors to get confidence in their simulation data. However, when calculating the ρ_c critical density at percolation and the V_{ex} excluded volume of the sticks

$$\rho_c = \frac{1}{V_{ex}} \quad (2)$$

$$V_{ex} = (32\pi/3)r^3 + 8\pi Lr^2 + 4L^2r \langle \sin(\gamma) \rangle \quad (3)$$

they calculate the average of $\sin(\gamma)$ (γ the angle between two randomly positioned sticks) for the right isotropic

case, getting $\langle \sin(\gamma) \rangle = \pi/4$. Calculating $\langle \sin(\gamma) \rangle$ for their "isotropic" configurations the result would be $\langle \sin(\gamma) \rangle = 2/\pi$. It is even more striking that in a following letter [4], confirming also the excluded volume theory, the authors do observe the systematic deviation of the Monte Carlo results [1] for the isotropic case respective to the excluded volume rule (Fig. 2 in Ref. [4]), but they fail in explaining it. In Ref. [4] the authors argue that the systematic deviation is due to the fact that much smaller aspect ratios are required to get the right $r/L \rightarrow 0$ limit. The difference however, is obvious and in perfect agreement with our previous affirmations. The real value of $\langle \sin(\gamma) \rangle$ for the "isotropic" Monte Carlo simulations [1] should be $2/\pi$, which is approximately 1.24 times smaller than the value used ($\pi/4$), and the systematic deviation [4] in Fig.2 is just of this order in the right direction. The error in generating the right isotropic distribution is repeated in a rapid publication [5], where the authors study by Monte Carlo methods the cluster structure and conductivity of three-dimensional continuum systems. The simulation data for the isotropic system [1] is used in a series of other papers [6–10], where some tables and comparison with analytical results should be reconsidered.

New MC simulation considered by generating the right isotropic configuration confirm nicely the excluded volume theory. We will discuss our new simulation data and the simulation procedure in a regular paper.

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